



MICROCOPY RESOLUTION TEST CHART NATIONAL BUPLAU OF 514NDARDS (463.4

. .

•

• ••

• •

Technical Report No. R-4-82

Project; Task No. 61102F; 2301/A3

Date: December 1, 1982

<u>Title</u>: <u>Exciton-Laser Amplifier</u>

Authors: Richard L. Liboff

K. C. Liu

Contractor: Cornell University

Principal Investigator: Richard L. Liboff

Research supported in part by the Air Force office of Scientific Research under contract AFOSR-78-3574. Distribution of this report is unlimited.

Approved for y thing of most

SECURITY CLASSIFIC AND OF WHIS PAGE (When Date Entered)

REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM	
1. REPORT NUMBER 2. GOVT ACCESSION NO	. 3. RECIPIENT'S CATALOG NUMBER	
AFOSR TR 0.544		
4. TITLE (and Subtitle)	5. TYPE OF REPORT & PERIOD COVERED	
Exciton-Laser Amplifier	Interim	
	6. PERFORMING ORG. REPORT NUMBER	
7. AUTHOR(#)	8. CONTRACT OR GRANT NUMBER(#)	
Richard L. Liboff K.C. Liu	AFOSR 78-3574	
K.G. Eld	1	
9. PERFORMING ORGANIZATION NAME AND ADDRESS	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS	
Cornell University	61102F	
Ithaca, N.Y. 14853	2301/A3	
11. CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE	
Directorate of Physics	Dec. 1, 1982	
AFOSR	13. NUMBER OF PAGES	
Bolling AF Base, D.C. 20332	Eight	
14. MONITORING AGENCY NAME & ADDRESS(If different from Controlling Office)	15. SECURITY CLASS. (of this report)	
	Unclassified	
	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE	

16. DISTRIBUTION STATEMENT (of this Report)

Approved for public release: distribution unlimited.

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)

Approved for Public Release; Distribution Unlimited

18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

Laser. Laser amplifier, Excitons, Pure crystals. Semiconductors, Insulators, Gain. Stimulated decay. Non-bose like excitons.

20. AESTRACT (Continue on reverse side if necessary and identify by block number)

A laser-amplifying device is described which is based on the simulated decay of excitons in a pure crystal. An estimate is made of the gain of the device. At a typical frequency the gain is found to be appreciably large thus suggesting practical application of the laser amplifier.

DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE

UNULAS

Abstract

A laser-amplifying device is described which is based on the stimulated decay of excitons in a pure crystal. An estimate is made of the gain of the device. At a typical frequency the gain is found to be appreciably large thus suggesting practical application of the laser amplifier.

AIR FORTE Of the service of the serv

In a previous article by the authors [1], a lasing mechanism was described based on stimulated decay of excitons. The process depends critically on the non-boson quality of excitons, which in turn may be assured by sufficiently high exciton density. This criterion follows from the fact that the ideal bose commutation relations [2] become increasingly invalid with growth of the number of excited atoms in the crystal.

In the present paper a laser-amplifying device is proposed based on the process described above. Namely, it is proposed that excitons in a pure (insulator or semiconductor) crystal are triggered by incident resonant laser radiation and that excitons are created by an external intermittent radiative source.

Thus, for example [3], exciton decay wavelength in pure ZnS is 3201.71~Å. The crystal could then be used to amplify radiation stemming from a dye laser at the same wavelength. Other characteristic wavelengths appropriate to this device are listed in Table 1.

The device is modeled as follows: Excitons in the pure crystal are created by a flash lamp. The power supply to the lamp has an on-off profile which is  $\pi$  radians out of phase with the pulse frequency of the input laser. The duration between peaks of this profile is of the order of the lifetime of an exciton, ~10<sup>-6</sup> sec.

We assume this modulation has the following effect. Exciton density grows during the 'on' phase of the lamp to a peak value

and then suffers resonant stimulated decay by the input laser radiation during the 'off' phase of the lamp.

During the amplification interval, radiative power flux,  $S[\text{W/m}^2],$  in the crystal satisfies the equation

$$\frac{dS}{dx} = g S \tag{1}$$

where g is the gain,

$$g = \kappa (\rho \sigma_{d} - \rho_{o} \sigma_{a}) \tag{2}$$

In this expression  $\rho$  is density of excited atoms, and  $\rho_0$  is density of atoms in the general state. It follows that the total density of atoms,  $\rho_T$ , is given by

$$\rho_{\mathbf{T}} = \rho + \rho_{\mathbf{O}}$$

The absorption cross section is  $\sigma_a$  and  $\sigma_d$  is the cross section for stimulated decay. Finally  $\kappa$  describes additional loss effects such as, for example, that due to reflection, impurities, missmatch between input and resonant frequencies, etc.

From the principle of microscopic reversibility [4] and assuming non-degeneracy of excited and ground exciton levels, one may set  $\sigma_d = \sigma_a$ . Furthermore, for  $\sigma$  we may write [5]

$$\sigma(\omega) = \frac{(2\pi)^2 e^2 \omega g_L(\omega) d^2}{3\hbar c}$$
 (4)

Here d is the dipole matrix element between Wannier state functions. At the site d it is given by

$$d = \langle c \ell \mid r \mid y \ell \rangle. \tag{5}$$

Valence and conduction bands are denoted by v and c respectively.

This matrix element is relevant to a transition between the ground and excited states of an exciton.

The term  $g_L$  in (4) refers to the Lorentzian lineshape factor. On resonance it reduces to [5]

$$g_{L} = \frac{\tau}{\pi} \tag{6}$$

In this expression  $\tau$  denotes the decay time of the exciton. As previously noted,  $\tau \simeq 10^{-6}$  sec.

A rough estimate of the matrix element (5) may be constructed as follows. We assume that the valence band is comprised of S atomic states and the conduction band is comprised of P atomic states. With

$$s \equiv r - \ell$$
,

in the coordinate representation, the bra and ket vectors in (5) become, respectively,

$$W_{v}(s) = \frac{1}{\sqrt{4\pi} a^{3/2}} e^{-s/a}$$

$$W_{c}(s) = \frac{s e^{-s/2a}}{(2a)^{3/2} a \sqrt{3}} \sqrt{\frac{3}{4\pi}} \cos\theta$$
(7)

where  $\cos \theta = \hat{z} \cdot \hat{s}/s$ , for an arbitrary z-axis. Furthermore,

$$a = \epsilon a_0^* = \epsilon \hbar^2/m^*e^2$$

where  $\epsilon$  is the dielectric constant.

There results

$$d = \left(\frac{2}{3}\right)^{6} a \frac{1}{\sqrt{8}} \int_{0}^{\infty} ds \, s^{4} e^{-3s/2a}$$

$$= \frac{2^{8}}{\sqrt{2} \cdot 3^{5}} a$$
(8)

with (6) and (8),  $\sigma$  as given by (4) becomes

$$\sigma = 32\pi \left(\frac{2}{3}\right)^8 \alpha \omega \tau a^2 \tag{9}$$

where  $\alpha$  is the fine structure constant.

Returning to (2), with (9) we write

$$g = 32\pi \left(\frac{2}{3}\right)^8 \alpha \omega \tau a^2 \kappa (\rho - \rho_0)$$
 (10)

At 55% pumping efficiency,  $\rho$  = 0.55  $\rho_{T}$ ,  $\rho_{O}$  = 0.45  $\rho_{T}$  and (10) reduces to

$$g = 32\pi \left(\frac{2}{3}\right)^8 \alpha \omega \tau a^2 0.1 \kappa \rho_T$$
 (11)

At  $\omega \simeq 10^{14}$ ,  $\tau \simeq 10^{-6}$ , a  $\simeq 0.5$  Å we find

$$g \simeq 7.16 \times 10^{-9} \kappa \rho_{T} \tag{12}$$

Thus for  $\kappa \rho_T > 10^9$ , g > 1 and the device may be expected to amplify the input laser pulse.

We have described a laser-amplifier device based on stimulated decay of excitons in a pure crystal. An expression for the gain of the device together with a criterion for amplification were obtained. These expressions suggest practical use of the proposed device. The device presumes a non-bose like quality of excitons. This property is satisfied provided a sufficiently large number of atoms are excited, i.e.,  $\rho \gtrsim \rho_{\rm O}$ .

This research was supported in part under contract AFOSR 78-3574.

## References

- [1] K.C. Liu and R.L. Liboff, "Criterion for Exciton Lasing in Pure Crystals", submitted to J. Appl. Phys.
- [2] J.J. Hopfield, "Theory of the Contribution of Excitons to the Complex Dielectric Constant of Crystals", Phys. Rev. 112 1555-1567, 1958.
- [3] D.C. Reynolds and T.C. Collins, "Excitons: Their Properties and Uses", Academic Press, New York, 1981.
- [4] R.L. Liboff, "Introductory Quantum Mechanics", Holden Day, Oakland, CA (1980).
- [5] R.H. Pantell and H.E. Puthoff, "Fundamentals of Quantum Electronics", John Wiley, New York, 1969.

Table 1

Characteristic Exciton Properties in Selected Crystals [3]

Material	Energy gap E (meV)	Binding energy E <sub>b</sub> (meV)	Photon energy E <sub>g</sub> -E <sub>b</sub> (meV)	Wavelength (Å)
Si	1112	14	1098	11290.5 (IR)
Ge	803	3.6	799.4	15507.9 (IR)
Zn0	3436	59	3377	3671.01 (V)
ZnS	3911	39	3872	3201.71 (UV)
ZnSe	2795	281	2514	4931.2 (0)
GaAs	1519	4.2	1514.8	8183.9 (IR)
CdS	2582	28	2554	4853.9 (0)
InSb	235.2	0.4	234.8	52798.1 (IR)

(IR, 0, V, UV)  $\equiv$  (infrared, optical, violet, ultraviolet)

FILMED

(A)